## <u>Introduction</u>

The Math Test Specifications provide an overview of the structure and content of Ohio's State Test. This overview includes a description of the test design as well as information on the types of items that will appear on the test. Also included is a test blueprint, a document that identifies the range and distribution of points grouped into various reporting categories (e.g., Fractions, Ratios and Proportions, Functions, Probability). The specifications also provide specific guidelines for the development of all items used for Ohio's math tests. This document is a resource not only for item writers and test designers, but also for Ohio educators and other stakeholders who are interested in a deeper understanding of the test.

## Overview of Structure and Content

#### Ohio's Learning Standards

In 2017, Ohio adopted revisions to <u>Ohio's Learning Standards for Mathematics</u> which include standards for mathematical content and mathematical practice. Then, based on the 2017 Standards, Ohio adopted revisions to the <u>Model Curriculum</u>, a document that connects standards to instruction. The mathematics assessment items (test questions) align to the 2017 Standards.

#### Standards for Mathematical Practice

The <u>Standards for Mathematical Practice</u> (SMP) describe skills that mathematics educators at all levels should seek to develop in their students. These practices rest on important "processes and proficiencies" with longstanding importance in mathematics education. The design of each item on Ohio's state tests encourages students to use one or more Standards for Mathematical Practice. Below is a list of the mathematical practices.

# Geometry Standards for Mathematical Practice Make sense of problems and persevere in solving them. Reason abstractly and quantitatively. Construct viable arguments and critique the reasoning of others. Model with mathematics. Use appropriate tools strategically. Attend to precision. Look for and make use of structure.

8. Look for and express regularity in repeated reasoning.

# **Blueprint**

<u>Test blueprints</u> serve as a guide for test construction and provide an outline of the content and skills to be measured on the test. They contain information about the number of points of opportunity students will encounter in each reporting category on the math test. The following test blueprint displays the distribution of the content standards and depth of knowledge across the entire test and categories for reporting test results for Geometry.

Reporting Category		Stan	dards		Approximate Portion of Test	
	G.CO.1	G.CO.6	G.CO.11	G.GPE.4		]
	G.CO.2	G.CO.7	G.CO.12	G.GPE.5	33% – 39%	
Congruence and Proof	G.CO.3	G.CO.8	G.CO.13	G.GPE.6		
	G.CO.4	G.CO.9	G.CO.14	G.GPE.7	19 – 21 points	
	G.CO.5	G.CO.10				
	G.SRT.1	G.SRT.5	G.MG.1	G.GMD.5	23% – 35%	
Similarity & Trigonometry	G.SRT.2	G.SRT.6	G.MG.2	G.GMD.6		\
ingeneria,	G.SRT.3	G.SRT.7	G.MG.3		13 – 19 points	Modeling and Reasoning*
	G.SRT.4	G.SRT.8a				(minimum 20%)
	G.C.1	G.GPE.1	G.GMD.1			1 / (
Circles	G.C.2		G.GMD.3		18% – 24%	
Circles	G.C.3		G.GMD.4		10 – 13 points	
	G.C.5					
	S.CP.1	S.CP.4	S.CP.6		18% – 22%	
Probability	S.CP.2	S.CP.5	S.CP.7			
	S.CP.3				10 – 12 points	IJ
			Т	otal Test	54 – 56 points	

Depth of Knowledge (DOK) Level	Approximate Portion of Test
1	8 – 16 points
2	25 – 40 points
3	8 – 16 points

#### **Modeling and Reasoning**

<u>Modeling and Reasoning</u> are included in the eight Standards for Mathematical Practice within Ohio's Learning Standards. Each grade's blueprint identifies modeling and reasoning as an independent reporting category that will account for a minimum of 20 percent of the overall points on that grade's test.

Modeling is best interpreted not as a collection of isolated topics but in relation to other standards. Making mathematical models is a Standard for Mathematical Practice, and specific modeling standards appear throughout the high school standards indicated by a star symbol (\*).

#### Depth of Knowledge (DOK)

<u>DOK</u> refers to the complexity of thinking required to complete a task in a given item. Items with a DOK 1 designation focus on the recall of information, such as definitions and terms, and simple procedures. Items with a DOK 2 designation require students to make decisions, solve routine problems, perform calculations, or recognize patterns. Items with a DOK 3 designation feature higher-order cognitive tasks. These DOK 3 tasks include but are not limited to: critiquing a statement and forming a conclusion; explaining, justifying, or proving a statement; or approaching abstract, complex, open-ended, and non-routine problems. Each grade's blueprint contains information about the number of points of opportunity students will encounter at each DOK level.

# **Test Design**

The assessment is a two-part test, developed in a computer-based format and a paper-based format. Its purpose is to measure student progress and provide information to parents, teachers, and building, district and state administrators. The test will contain technology-enhanced items that require the student to enter a response into the computer interface. The test will be administered near the end of the academic school year or the end of a semester (for high school). The test can be administered in one or two sessions. After the student has completed both parts of the test, his or her scores will be combined to yield a comprehensive test score. Test results are reported back to schools by June 30th.

### Performance Level Descriptors (PLDs)

At each grade level/course, <u>PLDs</u> are general statements describing what students should know or be able to do at each performance level.

After the Ohio State Mathematics test is scored, each student's performance level is identified based on the combined scores (Part 1 and Part 2). Districts and schools are sent item level reports and the performance level for each student along with the performance level descriptors. Teachers and math coaches can use this information for their instructional design.

#### Calculator

Calculators are **not** permitted for use on either the paper-based or computer-based mathematics test for grades 3-5. Grades 6 and 7 have a non-calculator part and a calculator part for both the paper-based and the computer-based mathematics test. The calculator designation for items in grades 6 and 7 is decided during development on an item-by-item basis. A calculator may be used on the entire grade 8 and high school End of Course (EOC) paper-based or computer-based mathematics tests. Note that calculator usage may differ for those students with an Individualized Education Plan (IEP) or 504 plan that specifies a calculator accommodation.

- Guidance on Desmos Calculator for Grades 3-8
- Grades 3-8 Handheld Calculator Guidance
- Guidance on Desmos Calculator for High School
- High School Handheld Calculator Guidance

#### Reference Sheets

A <u>reference sheet</u> may be used on the Ohio State Mathematics Tests by all students in grades four and above. For paper-based testers, the math reference sheets will be included within the student test booklet. For online testers, the math reference sheet is embedded within the testing platform.

## **Interaction Types**

Ohio's State Tests are composed of several interaction types. Currently, there are ten interaction types that may appear on a math computer-based assessment:

- Equation Item (EQ)
- Gap Match Item (GM)
- Grid Item (GI)
- Hot Text Item (HT)
- Inline Choice Item (IC)
- Matching Item (MI)
- Multiple Choice Item (MC)
- Multi Select Item (MS)
- Simulation Item (Sim)
- Table Item (TI)

For paper-based assessments (including those for students with an IEP or 504 plan that specifies a paper-based accommodation), the items may be modified so that they can be scanned and scored electronically or hand-scored.

Interaction Type	Description
Equation Item (EQ)	The student is presented with a keypad that includes a variety of mathematical symbols that can be used to create a response. Responses may be in the form of a number, variable, expression, or equation, as appropriate to the test item. The student enters their response in the response box which may be on a line by itself, or embedded in a sentence or phrase. For paper-based assessments, this interaction type may be replaced with a modified version of the item that can be scanned and scored electronically or the student may be given an answer box to write their answer.
Gap Match  Item  (GM)	Given a set of options (e.g., numbers, words, phrases, or sentences) the student hovers over the options which then highlight, indicating that the option is selectable. The student can then click on the object, hold down the mouse button, and drag it to an answer area, indicated by a dotted box, in a graphic, table, or paragraph. For paper-based assessments, the options are associated with a letter, and students write a letter for their response in each response area.
Grid Item (GI)	The student may select numbers, words, phrases, or images to display their response. The student may also use the drag-and-drop feature to place objects into a response area. This interaction type may also require the student to use the point, line, or arrow tools to create a response on a graph or gridded area. For paper-based assessments, the student may be given the response space to draw their answer, or this interaction type may be replaced with another interaction type that assesses the same standard at the same level of difficulty and can be scanned and scored electronically.
Hot Text Item (HT)	Selectable Hot Text - Given a set of options (e.g., phrases, sentences, or numbers) the student hovers over the options which then highlight, indicating that the text is selectable ("hot"). The student can then click on an option to select it as their response. For paper-based assessments, a "selectable" hot text item is modified so that it can be scanned and scored electronically. The student fills in a circle to indicate the correct response.
	<b>Drag-and-Drop Hot Text</b> - Given a set of options (e.g., numbers, words, phrases, or sentences) the student hovers over the options which then highlight, indicating that the option is selectable ("hot"). The student can then click on the object, hold down the mouse button, and drag it to a graphic, table, or paragraph. For paper-based assessments, the options are associated with a letter, and students write a letter for their response in each response area.

Interaction Type	Description
Inline Choice Item (IC)	Given a sentence, paragraph, or table, the student clicks a blank box embedded within a sentence or table which reveals a drop-down menu containing options for completing a sentence or table. The student then selects an option from the drop-down menu to respond. For paper-based assessments, the interaction is modified so that it can be scanned and scored electronically. The student fills in a circle to indicate the correct response.
Matching Item (MI)	Given column and row headers in a table format, the student checks a box to indicate if information from a column header matches information from a row header. For paper-based assessments, the interaction is modified so that it can be scanned and scored electronically. The student fills in a circle to indicate the correct response.
Multiple Choice Item (MC)	The student selects one correct answer from four options. For paper-based assessments, the student fills in a circle to indicate the correct response.
Multi Select  Item  (MS)	The student is directed to either select an indicated number of correct answers or to select all of the correct answers. Students in grades 3-5 always select an indicated number of correct answers; students in grades 6-8 select an indicated number of correct answers on 50% of the items and select all on 50% of the items; and students taking high school end-of-course tests are always directed to select all correct answers. These items are different from multiple choice items, and require the student to select 2 or more correct answers. For paper-based assessments, the student fills in circles to indicate the correct responses.
Simulation Item (Sim)	Given a set of instructions, the student may interact with any of the following controls to generate data: radio buttons, drop-down menus, slide bars, or selecting a number by clicking arrows. Once the student has set the parameters, they click the start button to begin the simulation and generate a data set. Once the student has enough data, they may answer questions about the data using a different interaction type. For paper-based assessments, this interaction will be replaced with another interaction type that assesses the same standard at the same level of difficulty and can be scanned and scored electronically.
Table Item (TI)	The student types numeric values into a given table. The student may complete the entire table or portions of the table depending on what is being asked. For paper-based assessments, the student writes their responses in the blank boxes of the table.

# Specific Guidelines for Item Development

Standards are presented according to reporting categories as shown on grade level or course blueprints.

Reporting Category	CONGRUENCE AND PROOF
Content Standard	G.CO CONGRUENCE
	Experiment with transformations in the plane.
	<b>G.CO.1</b> Know precise definitions of ray, angle, circle, perpendicular line, parallel line, and line segment, based on the undefined notions of point, line, distance along a line, and arc length.
Content Limits	None
DOK	1, 2, and/or 3 are eligible. DOK levels are designated on an item-by-item basis.
Context	Context Optional

Reporting Category	CONGRUENCE AND PROOF
Content Standard	G.CO CONGRUENCE
	Experiment with transformations in the plane.
	<b>G.CO.2</b> Represent transformations in the plane using, e.g., transparencies and geometry software; describe transformations as functions that take points in the plane as inputs and give other points as outputs. Compare transformations that preserve distance and angle to those that do not, e.g., translation versus horizontal stretch.
Content Limits	<ul> <li>Transformations limited to the following:         <ul> <li>dilations with a positive scale factor and an indicated center of dilation</li> <li>translations</li> <li>rotations with an indicated center of rotation</li> <li>reflections across lines (lines of reflections may be lines other than a horizontal line, vertical line, y = x, or y = -x)</li> </ul> </li> <li>Items may involve multiple transformations.</li> <li>Items may require the student to identify or create a rule using ordered pair notation to describe a series of transformations for any point (x, y).</li> </ul>
DOK	1, 2, and/or 3 are eligible. DOK levels are designated on an item-by-item basis.
Context	Context Optional

Reporting Category	CONGRUENCE AND PROOF
Content Standard	G.CO CONGRUENCE
	Experiment with transformations in the plane.
	<b>G.CO.3</b> Identify the symmetries of a figure, which are the rotations and reflections that carry it onto itself.
	<u>G.CO.3a</u> Identify figures that have line symmetry; draw and use lines of symmetry to analyze properties of shapes.
	<u>G.CO.3b</u> Identify figures that have rotational symmetry; determine the angle of rotation, and use rotational symmetry to analyze properties of shapes.
Content Limits	None
DOK	1, 2, and/or 3 are eligible. DOK levels are designated on an item-by-item basis.
Context	Context Optional

Reporting Category	CONGRUENCE AND PROOF
Content Standard	G.CO CONGRUENCE
	Experiment with transformations in the plane.
	<b>G.CO.4</b> Develop definitions of rotations, reflections, and translations in terms of angles, circles, perpendicular lines, parallel lines, and line segments.
Content Limits	None
DOK	1, 2, and/or 3 are eligible. DOK levels are designated on an item-by-item basis.
Context	Context Optional

Reporting Category	CONGRUENCE AND PROOF
Content Standard	G.CO CONGRUENCE
	Experiment with transformations in the plane.
	<b>G.CO.5</b> Given a geometric figure and a rotation, reflection, or translation, draw the transformed figure using items such as graph paper, tracing paper, or geometry software. Specify a sequence of transformations that will carry a given figure onto another.
Content Limits	<ul> <li>Transformations limited to the following:         <ul> <li>dilations with a positive scale factor and an indicated center of dilation</li> <li>translations</li> <li>rotations with an indicated center of rotation</li> <li>reflections across lines (lines of reflections may be lines other than a horizontal line, vertical line, y = x, or y = -x)</li> </ul> </li> <li>Items may require the student to identify or create a rule using ordered pair notation to describe a series of transformations for any point (x, y).</li> </ul>
DOK	1, 2, and/or 3 are eligible. DOK levels are designated on an item-by-item basis.
Context	Context Optional

Reporting Category	CONGRUENCE AND PROOF		
Content Standard	G.CO CONGRUENCE		
	Understand congruence in terms of rigid motions.		
	<b>G.CO.6</b> Use geometric descriptions of rigid motions to transform figures and to predict the effect of a given rigid motion on a given figure; given two figures, use the definition of congruence in terms of rigid motions to decide if they are congruent.		
Content Limits	<ul> <li>Transformations limited to the following:         <ul> <li>translations</li> <li>rotations with an indicated center of rotation</li> <li>reflections across lines (lines of reflections may be lines other than a horizontal line, vertical line, y = x, or y = -x)</li> </ul> </li> <li>Dilations may appear in selected response items as distractors. If used, the dilations would have a positive scale factor and an indicated center of dilation.</li> <li>Items may involve multiple transformations.</li> <li>Items may require the student to identify or create a rule using ordered pair notation to describe a series of transformations for any point (x, y).</li> <li>Items that describe the connection between congruence and transformations should assess knowledge of this line of reasoning - "Two shapes are congruent if one can be mapped onto another using reflections, rotations, translations, and/or dilations with scale factor 1 on the other. All of these transformations maintain angle measure and side lengths.  Therefore, congruent figures have equal corresponding angle measures and equal corresponding pairs of side lengths.</li> </ul>		
DOK	1, 2, and/or 3 are eligible. DOK levels are designated on an item-by-item basis.		
Context	Context Optional		

Reporting Category	CONGRUENCE AND PROOF	
Content Standard	G.CO CONGRUENCE	
	Understand congruence in terms of rigid motions.	
	<b>G.CO.7</b> Use the definition of congruence in terms of rigid motions to show that two triangles are congruent if and only if corresponding pairs of sides and corresponding pairs of angles are congruent.	
Content Limits	<ul> <li>Transformations limited to translations, rotations, and reflections, although dilations may appear in selected response items as distractors.</li> <li>Items may involve multiple transformations.</li> <li>Items may require the student to identify or create a rule using ordered pair notation to describe a series of transformations for any point (x, y).</li> </ul>	
DOK	1, 2, and/or 3 are eligible. DOK levels are designated on an item-by-item basis.	
Context	Context Optional	

Reporting Category	CONGRUENCE AND PROOF	
Content Standard	G.CO CONGRUENCE	
	Understand congruence in terms of rigid motions.	
	<b>G.CO.8</b> Explain how the criteria for triangle congruence (ASA, SAS, and SSS) follow from the definition of congruence in terms of rigid motions.	
Content Limits	<ul> <li>Transformations limited to translations, rotations, and reflections, although dilations may appear in selected response items as distractors.</li> <li>Items may involve multiple transformations.</li> <li>Items may require the student to identify or create a rule using ordered pair notation to describe a series of transformations for any point (x, y).</li> </ul>	
DOK	1, 2, and/or 3 are eligible. DOK levels are designated on an item-by-item basis.	
Context	Context Optional	

Reporting Category	CONGRUENCE AND PROOF
Content Standard	G.CO CONGRUENCE
	Prove geometric theorems both formally and informally using a variety of methods.
	<b>G.CO.9</b> Prove and apply theorems about lines and angles. Theorems include but are not restricted to the following: vertical angles are congruent; when a transversal crosses parallel lines, alternate interior angles are congruent and corresponding angles are congruent; points on a perpendicular bisector of a line segment are exactly those equidistant from the segment's endpoints.
Content Limits	<ul> <li>Proving methods include, but are not restricted to, two-column proofs, flow chart proofs, paragraph/narrative proofs, indirect proofs, and transformational proofs.</li> <li>The formal names of properties and theorems need to be recognized to justify statements (Note: The Addition Property of Equality and Multiplication Property of Equality can be used instead of the Subtraction Property of Equality and Division Property of Equality, respectively).</li> </ul>
DOK	1, 2, and/or 3 are eligible. DOK levels are designated on an item-by-item basis.
Context	Context Optional

Reporting Category	CONGRUENCE AND PROOF
Content Standard	G.CO CONGRUENCE
	Prove geometric theorems both formally and informally using a variety of methods.
	<b>G.CO.10</b> Prove and apply theorems about triangles. Theorems include but are not restricted to the following: measures of interior angles of a triangle sum to 180°; base angles of isosceles triangles are congruent; the segment joining midpoints of two sides of a triangle is parallel to the third side and half the length; the medians of a triangle meet at a point.
Content Limits	<ul> <li>Proving methods include, but are not restricted to, two-column proofs, flow chart proofs, paragraph/narrative proofs, indirect proofs, coordinate proofs, and transformational proofs.</li> <li>The formal names of properties and theorems need to be recognized to justify statements (Note: The Addition Property of Equality and Multiplication Property of Equality can be used instead of the Subtraction Property of Equality and Division Property of Equality, respectively).</li> </ul>
DOK	1, 2, and/or 3 are eligible. DOK levels are designated on an item-by-item basis.
Context	Context Optional

Reporting Category	CONGRUENCE AND PROOF
Content Standard	G.CO CONGRUENCE
	Prove geometric theorems both formally and informally using a variety of methods.
	<b>G.CO.11</b> Prove and apply theorems about parallelograms. Theorems include but are not restricted to the following: opposite sides are congruent, opposite angles are congruent, the diagonals of a parallelogram bisect each other, and conversely, rectangles are parallelograms with congruent diagonals.
Content Limits	<ul> <li>Proving methods include, but are not restricted to, two-column proofs, flow chart proofs, paragraph/narrative proofs, indirect proofs, and transformational proofs.</li> <li>The formal names of properties and theorems need to be recognized to justify statements (Note: The Addition Property of Equality and Multiplication Property of Equality can be used instead of the Subtraction Property of Equality and Division Property of Equality, respectively).</li> </ul>
DOK	1, 2, and/or 3 are eligible. DOK levels are designated on an item-by-item basis.
Context	Context Optional

Reporting Category	CONGRUENCE AND PROOF
Content Standard	G.CO CONGRUENCE
	Make geometric constructions.
	<b>G.CO.12</b> Make formal geometric constructions with a variety of tools and methods (compass and straightedge, string, reflective devices, paper folding, dynamic geometric software, etc.). Copying a segment; copying an angle; bisecting a segment; bisecting an angle; constructing perpendicular lines, including the perpendicular bisector of a line segment; and constructing a line parallel to a given line through a point not on the line.
Content Limits	Items may require the student to justify steps and results.
DOK	1, 2, and/or 3 are eligible. DOK levels are designated on an item-by-item basis.
Context	Context Optional

Reporting Category	CONGRUENCE AND PROOF
Content Standard	G.CO CONGRUENCE
	Make geometric constructions.
	<b>G.CO.13</b> Construct an equilateral triangle, a square, and a regular hexagon inscribed in a circle.
Content Limits	Items may require the student to justify steps and results.
DOK	1, 2, and/or 3 are eligible. DOK levels are designated on an item-by-item basis.
Context	Context Optional

Reporting Category	CONGRUENCE AND PROOF
Content Standard	G.CO CONGRUENCE
	Classify and analyze geometric figures.
	G.CO.14 Classify two-dimensional figures in a hierarchy based on properties.
Content Limits	Possible two-dimensional figures include, but are not restricted to, triangles, quadrilaterals, and other polygons.  There are two definitions of a transposid, and that requires exactly one pair.
	<ul> <li>There are two definitions of a trapezoid – one that requires exactly one pair of parallel sides, and another that requires at least one pair of parallel sides. Items will not require the student to use one definition of a trapezoid over the other.</li> </ul>
	<ul> <li>There are two definitions of an isosceles triangle – one that requires exactly two sides of the same length, and another that requires at least two sides of the same length. Items will not require the student to use one definition of an isosceles triangle over the other.</li> </ul>
DOK	1, 2, and/or 3 are eligible. DOK levels are designated on an item-by-item basis.
Context	Context Optional

Reporting Category	CONGRUENCE AND PROOF
Content Standard	G.GPE EXPRESSING GEOMETRIC PROPERTIES WITH EQUATIONS
	Use coordinates to prove simple geometric theorems algebraically and to verify specific geometric statements.
	<b>G.GPE.4</b> Use coordinates to prove simple geometric theorems algebraically and to verify geometric relationships algebraically, including properties of special triangles, quadrilaterals, and circles. For example, determine if a figure defined by four given points in the coordinate plane is a rectangle; determine if a specific point lies on a given circle. (G, M2)
Content Limits	<ul> <li>All four quadrants of the coordinate plane may be used.</li> <li>Items may use radical values.</li> <li>Include simple proofs involving circles, properties of quadrilaterals, and special right triangles (30-60-90 and 45-45-90)</li> <li>Proving methods include, but are not restricted to, two-column proofs, flow chart proofs, paragraph/narrative proofs, indirect proofs, coordinate proofs, and transformational proofs.</li> <li>The formal names of properties and theorems need to be recognized to justify statements in some proofs (Note: The Addition Property of Equality and Multiplication Property of Equality can be used instead of the Subtraction Property of Equality and Division Property of Equality, respectively).</li> <li>Items may require the application of the distance formula.</li> </ul>
DOK	1, 2, and/or 3 are eligible. DOK levels are designated on an item-by-item basis.
Context	Context Optional

Reporting Category	CONGRUENCE AND PROOF
Content Standard	G.GPE EXPRESSING GEOMETRIC PROPERTIES WITH EQUATIONS
	Use coordinates to prove simple geometric theorems algebraically and to verify specific geometric statements.
	<b>G.GPE.5</b> Justify the slope criteria for parallel and perpendicular lines, and use them to solve geometric problems, e.g., find the equation of a line parallel or perpendicular to a given line that passes through a given point.
Content Limits	<ul> <li>All four quadrants</li> <li>Proving methods include, but are not restricted to, two-column proofs, flow chart proofs, paragraph/narrative proofs, indirect proofs, coordinate proofs, and transformational proofs.</li> <li>The formal names of properties and theorems need to be recognized to justify statements in some proofs (Note: The Addition Property of Equality and Multiplication Property of Equality can be used instead of the Subtraction Property of Equality and Division Property of Equality, respectively).</li> </ul>
DOK	1, 2, and/or 3 are eligible. DOK levels are designated on an item-by-item basis.
Context	Context Optional

Reporting Category	CONGRUENCE AND PROOF
Content Standard	G.GPE EXPRESSING GEOMETRIC PROPERTIES WITH EQUATIONS
	Use coordinates to prove simple geometric theorems algebraically and to verify specific geometric statements.
	<b>G.GPE.6</b> Find the point on a directed line segment between two given points that partitions the segment in a given ratio.
Content Limits	None
DOK	1, 2, and/or 3 are eligible. DOK levels are designated on an item-by-item basis.
Context	Context Optional

Reporting Category	CONGRUENCE AND PROOF
Content Standard	G.GPE EXPRESSING GEOMETRIC PROPERTIES WITH EQUATIONS
	Use coordinates to prove simple geometric theorems algebraically and to verify specific geometric statements.
	<b>G.GPE.7</b> Use coordinates to compute perimeters of polygons and areas of triangles and rectangles, e.g., using the distance formula.★
Content Limits	<ul> <li>Items may involve polygons, triangles, rectangles, or use shapes composed of triangles and rectangles.</li> <li>At least part of the computation must require the application of the distance formula.</li> </ul>
DOK	1, 2, and/or 3 are eligible. DOK levels are designated on an item-by-item basis.
Context	Context Optional

Reporting Category	SIMILARITY AND TRIGONOMETRY
Content Standard	G.SRT SIMILARITY, RIGHT TRIANGLES, AND TRIGONOMETRY
	Understand similarity in terms of similarity transformations.
	<b>G.SRT.1</b> Verify experimentally the properties of dilations given by a center and a scale factor:
	<u>G.SRT.1a</u> A dilation takes a line not passing through the center of the dilation to a parallel line and leaves a line passing through the center unchanged.
	<u>G.SRT.1b</u> The dilation of a line segment is longer or shorter in the ratio given by the scale factor.
Content Limits	Scale factors are positive.
	<ul> <li>Items may involve polygons.</li> </ul>
	<ul> <li>Items may require the student to identify or create a rule using ordered pair notation to describe a series of transformations for any point (x, y).</li> <li>Items may require students to determine an equation of a line that is the result of dilating a given line.</li> </ul>
DOK	1, 2, and/or 3 are eligible. DOK levels are designated on an item-by-item basis.
Context	Context Optional

Reporting Category	SIMILARITY AND TRIGONOMETRY
Content Standard	G.SRT SIMILARITY, RIGHT TRIANGLES, AND TRIGONOMETRY
	Understand similarity in terms of similarity transformations.
	<b>G.SRT.2</b> Given two figures, use the definition of similarity in terms of similarity transformations to decide if they are similar; explain using similarity transformations the meaning of similarity for triangles as the equality of all corresponding pairs of angles and the proportionality of all corresponding pairs of sides.
Content Limits	<ul> <li>Transformations limited to the following:         <ul> <li>dilations with a positive scale factor and an indicated center of dilation</li> <li>translations</li> <li>rotations with an indicated center of rotation</li> <li>reflections across lines (lines of reflections may be lines other than a horizontal line, vertical line, y = x, or y = -x)</li> </ul> </li> <li>Items may require the student to identify or create a rule using ordered pair notation to describe a series of transformations for any point (x, y).</li> <li>Items that describe the connection between similarity and transformations should assess knowledge of this line of reasoning - "Two shapes are similar if one can be mapped onto another using reflections, rotations, translations, and/or dilations on the other. All of these transformations maintain angle measure and ratios of side lengths. Therefore, similar figures have equal corresponding angle measures and corresponding pairs of sides are proportional."</li> </ul>
DOK	1, 2, and/or 3 are eligible. DOK levels are designated on an item-by-item basis.
Context	Context Optional

Reporting Category	SIMILARITY AND TRIGONOMETRY
Content Standard	G.SRT SIMILARITY, RIGHT TRIANGLES, AND TRIGONOMETRY
	Understand similarity in terms of similarity transformations.
	<b>G.SRT.3</b> Use the properties of similarity transformations to establish the AA criterion for two triangles to be similar.
Content Limits	<ul> <li>Transformations limited to the following:         <ul> <li>dilations with a positive scale factor and an indicated center of dilation</li> <li>translations</li> <li>rotations with an indicated center of rotation</li> <li>reflections across lines (lines of reflections may be lines other than a horizontal line, vertical line, y = x, or y = -x)</li> </ul> </li> <li>Items may require the student to identify or create a rule using ordered pair notation to describe a series of transformations for any point (x, y).</li> </ul>
DOK	1, 2, and/or 3 are eligible. DOK levels are designated on an item-by-item basis.
Context	Context Optional

Reporting Category	SIMILARITY AND TRIGONOMETRY
Content Standard	G.SRT SIMILARITY, RIGHT TRIANGLES, AND TRIGONOMETRY
	Prove and apply theorems both formally and informally involving similarity using a variety of methods.
	<b>G.SRT.4</b> Prove and apply theorems about triangles. Theorems include but are not restricted to the following: a line parallel to one side of a triangle divides the other two proportionally, and conversely; the Pythagorean Theorem proved using triangle similarity.
Content Limits	<ul> <li>Proving methods include, but are not restricted to, two-column proofs, flow chart proofs, paragraph/narrative proofs, indirect proofs, coordinate proofs, and transformational proofs.</li> <li>The names of properties and theorems is needed to justify statements in proofs.</li> </ul>
DOK	1, 2, and/or 3 are eligible. DOK levels are designated on an item-by-item basis.
Context	Context Optional

Reporting Category	SIMILARITY AND TRIGONOMETRY
Content Standard	G.SRT SIMILARITY, RIGHT TRIANGLES, AND TRIGONOMETRY
	Prove and apply theorems both formally and informally involving similarity using a variety of methods.
	<b>G.SRT.5</b> Use congruence and similarity criteria for triangles to solve problems and to justify relationships in geometric figures that can be decomposed into triangles.
Content Limits	<ul> <li>Proving methods include, but are not restricted to, two-column proofs, flow chart proofs, paragraph/narrative proofs, indirect proofs, coordinate proofs, and transformational proofs.</li> </ul>
	<ul> <li>The names of properties and theorems is needed to justify statements in proofs.</li> </ul>
	<ul> <li>Items are limited to using SSS, SAS, ASA, AAS, and/or HL for congruence.</li> <li>Items use AA, SAS (ratios), and/or SSS (ratios) for similarity.</li> </ul>
	<ul> <li>Items may use geometric figures of any shape if the figure can be deconstructed to form a triangle.</li> </ul>
DOK	1, 2, and/or 3 are eligible. DOK levels are designated on an item-by-item basis.
Context	Context Optional

Reporting Category	SIMILARITY AND TRIGONOMETRY
Content Standard	G.SRT SIMILARITY, RIGHT TRIANGLES, AND TRIGONOMETRY
	Define trigonometric ratios, and solve problems involving right triangles.
	<b>G.SRT.6</b> Understand that by similarity, side ratios in right triangles are properties of the angles in the triangle, leading to definitions of trigonometric ratios for acute angles.
Content Limits	Trigonometric ratios are limited to sine, cosine, and tangent.
DOK	1, 2, and/or 3 are eligible. DOK levels are designated on an item-by-item basis.
Context	Context Optional

Reporting Category	SIMILARITY AND TRIGONOMETRY
Content Standard	G.SRT SIMILARITY, RIGHT TRIANGLES, AND TRIGONOMETRY
	Define trigonometric ratios, and solve problems involving right triangles.
	<b>G.SRT.7</b> Explain and use the relationship between the sine and cosine of complementary angles.
Content Limits	None
DOK	1, 2, and/or 3 are eligible. DOK levels are designated on an item-by-item basis.
Context	Context Optional

Reporting Category	SIMILARITY AND TRIGONOMETRY
Content Standard	G.SRT SIMILARITY, RIGHT TRIANGLES, AND TRIGONOMETRY
	Define trigonometric ratios, and solve problems involving right triangles.
	G.SRT.8 Solve problems involving right triangles.★
	<u>G.SRT.8a</u> Use trigonometric ratios and the Pythagorean Theorem to solve right triangles in applied problems if one of the two acute angles and a side length is given. (G, M2)
Content Limits	<ul> <li>Trigonometric ratios are limited to sine, cosine, and tangent.</li> <li>Items do not require the student to use inverse trigonometry functions to calculate unknown angle measures.</li> </ul>
DOK	1, 2, and/or 3 are eligible. DOK levels are designated on an item-by-item basis.
Context	Context Required

Reporting Category	SIMILARITY AND TRIGONOMETRY
Content Standard	G.MG MODELING WITH GEOMETRY  Apply geometric concepts in modeling situations.
	G.MG.1 Use geometric shapes, their measures, and their properties to describe objects, e.g., modeling a tree trunk or a human torso as a cylinder.★
Content Limits	None
DOK	1, 2, and/or 3 are eligible. DOK levels are designated on an item-by-item basis.
Context	Context Required

Reporting Category	SIMILARITY AND TRIGONOMETRY
Content Standard	G.MG MODELING WITH GEOMETRY
	Apply geometric concepts in modeling situations.
	G.MG.2 Apply concepts of density based on area and volume in modeling situations, e.g., persons per square mile, BTUs per cubic foot.★
Content Limits	Only some of these items should deal with density of an object. Others should deal with broader applications of the word density, like wolves per square mile.
DOK	1, 2, and/or 3 are eligible. DOK levels are designated on an item-by-item basis.
Context	Context Required

Reporting Category	SIMILARITY AND TRIGONOMETRY
Content Standard	G.MG MODELING WITH GEOMETRY
	Apply geometric concepts in modeling situations.
	<b>G.MG.3</b> Apply geometric methods to solve design problems, e.g., designing an object or structure to satisfy physical constraints or minimize cost; working with typographic grid systems based on ratios.★
Content Limits	<ul> <li>Items may require the student to use knowledge of other Geometry standards.</li> <li>Items that use volume should not also assess G.GMD.3 or G.MG.1.</li> </ul>
DOK	1, 2, and/or 3 are eligible. DOK levels are designated on an item-by-item basis.
Context	Context Required

Reporting Category	SIMILARITY AND TRIGONOMETRY
Content Standard	G.GMD GEOMETRIC MEASUREMENT AND DIMENSION
	Understand the relationships between lengths, area, and volumes.
	<b>G.GMD.5</b> Understand how and when changes to the measures of a figure (lengths or angles) result in similar and non-similar figures.
Content Limits	None
DOK	1, 2, and/or 3 are eligible. DOK levels are designated on an item-by-item basis.
Context	Context Optional

Reporting Category	SIMILARITY AND TRIGONOMETRY
Content Standard	G.GMD GEOMETRIC MEASUREMENT AND DIMENSION
	Understand the relationships between lengths, area, and volumes.
	<b>G.GMD.6</b> When figures are similar, understand and apply the fact that when a figure is scaled by a factor of $k$ , the effect on lengths, areas, and volumes is that they are multiplied by $k$ , $k^2$ , and $k^3$ , respectively.
Content Limits	None
DOK	1, 2, and/or 3 are eligible. DOK levels are designated on an item-by-item basis.
Context	Context Optional

Reporting Category	CIRCLES
Content Standard	G.C CIRCLES
	Understand and apply theorems about circles.
	<b>G.C.1</b> Prove that all circles are similar using transformational arguments.
Content Limits	Aside from items that ask the student to find the ratio of dilation between circles, items should focus on the fact that any circle can be obtained by a translation and dilation of any other circle.
DOK	1, 2, and/or 3 are eligible. DOK levels are designated on an item-by-item basis.
Context	Context Optional

Reporting Category	CIRCLES
Content Standard	G.C CIRCLES
	Understand and apply theorems about circles.
	<b>G.C.2</b> Identify and describe relationships among angles, radii, chords, tangents, and arcs and use them to solve problems. <i>Include the relationship between central, inscribed, and circumscribed angles and their intercepted arcs; inscribed angles on a diameter are right angles; the radius of a circle is perpendicular to the tangent where the radius intersects the circle.</i>
Content Limits	None
DOK	1, 2, and/or 3 are eligible. DOK levels are designated on an item-by-item basis.
Context	Context Optional

Reporting Category	CIRCLES
Content Standard	G.C CIRCLES
	Understand and apply theorems about circles.
	<b>G.C.3</b> Construct the inscribed and circumscribed circles of a triangle; prove and apply the property that opposite angles are supplementary for a quadrilateral inscribed in a circle.
Content Limits	<ul> <li>Items may involve the notions of incenter and circumcenter when referring to the intersection of a triangles angle bisectors or perpendicular segment bisectors.</li> </ul>
DOK	1, 2, and/or 3 are eligible. DOK levels are designated on an item-by-item basis.
Context	Context Optional

Reporting Category	CIRCLES
Content Standard	G.C CIRCLES
	Find arc lengths and areas of sectors of circles.
	G.C.5 Find arc lengths and areas of sectors of circles.
	<u>G.C.5a</u> Apply similarity to relate the length of an arc intercepted by a central angle to the radius. Use the relationship to solve problems.
	<u>G.C.5b</u> Derive the formula for the area of a sector, and use it to solve problems.
Content Limits	Items may involve composite shapes.
DOK	1, 2, and/or 3 are eligible. DOK levels are designated on an item-by-item basis.
Context	Context Optional

Reporting Category	CIRCLES
Content Standard	G.GPE EXPRESSING GEOMETRIC PROPERTIES WITH EQUATIONS
	Translate between the geometric description and the equation for a conic section.
	<b>G.GPE.1</b> Derive the equation of a circle of given center and radius using the Pythagorean Theorem; complete the square to find the center and radius of a circle given by an equation.
Content Limits	<ul> <li>All four quadrants of the coordinate plane</li> <li>Circle centers have integer coordinates.</li> <li>When completing the square, the emphasis is on cases where the leading coefficient is 1. When items use a leading coefficient other than 1 (such as -1, ±2, or ±3), the linear coefficient b is an integer evenly divisible by the leading coefficient a.</li> <li>When completing the square, the leading coefficient of each quadratic trinomial are equal so that both perfect square terms are divisible by the leading coefficient.</li> </ul>
DOK	1, 2, and/or 3 are eligible. DOK levels are designated on an item-by-item basis.
Context	Context Optional

Reporting Category	CIRCLES
Content Standard	G.GMD GEOMETRIC MEASUREMENT AND DIMENSION
	Explain volume formulas, and use them to solve problems.
	<b>G.GMD.1</b> Give an informal argument for the formulas for the circumference of a circle, area of a circle, and volume of a cylinder, pyramid, and cone. <i>Use dissection arguments, Cavalieri's principle, and informal limit arguments.</i>
Content Limits	Students should not be required to know informal arguments (Cavalieri's principle, dissection, etc.) by name.
DOK	1, 2, and/or 3 are eligible. DOK levels are designated on an item-by-item basis.
Context	Context Optional

Reporting Category	CIRCLES
Content Standard	G.GMD GEOMETRIC MEASUREMENT AND DIMENSION
	Explain volume formulas, and use them to solve problems.
	<b>G.GMD.3</b> Use volume formulas for cylinders, pyramids, cones, and spheres to solve problems.★
Content Limits	<ul> <li>Focus should be on solving real-world problems, not simply finding the volume of given figures.</li> <li>Items may use composite solids composed of cylinders, pyramids, cones, and spheres.</li> </ul>
DOK	1, 2, and/or 3 are eligible. DOK levels are designated on an item-by-item basis.
Context	Context Optional

Reporting Category	CIRCLES
Content Standard	G.GMD GEOMETRIC MEASUREMENT AND DIMENSION
	Visualize relationships between two-dimensional and three-dimensional objects.
	<b>G.GMD.4</b> Identify the shapes of two-dimensional cross-sections of three-dimensional objects, and identify three-dimensional objects generated by rotations of two-dimensional objects.
Content Limits	Items may use diagonal cross-sections.
DOK	1, 2, and/or 3 are eligible. DOK levels are designated on an item-by-item basis.
Context	Context Optional

Reporting Category	PROBABILITY
Content Standard	S.CP CONDITIONAL PROBABILITY AND THE RULES OF PROBABILITY
	Understand independence and conditional probability, and use them to interpret data.
	<b>S.CP.1</b> Describe events as subsets of a sample space (the set of outcomes) using characteristics (or categories) of the outcomes, or as unions, intersections, or complements of other events ("or," "and," "not").★
Content Limits	<ul> <li>Items use positive rational numbers to represent probabilities.</li> <li>Items may use Venn diagrams, tree diagrams, or frequency tables.</li> <li>Items may use union and intersection symbols.</li> </ul>
DOK	1, 2, and/or 3 are eligible. DOK levels are designated on an item-by-item basis.
Context	Context Optional

Reporting Category	PROBABILITY
Content Standard	S.CP CONDITIONAL PROBABILITY AND THE RULES OF PROBABILITY
	Understand independence and conditional probability, and use them to interpret data.
	<b>S.CP.2</b> Understand that two events A and B are independent if and only if the probability of A and B occurring together is the product of their probabilities, and use this characterization to determine if they are independent.★
Content Limits	<ul> <li>Items use positive rational numbers to represent probabilities.</li> <li>Items may use Venn diagrams, tree diagrams, or frequency tables.</li> <li>Items may use union and intersection symbols.</li> </ul>
DOK	1, 2, and/or 3 are eligible. DOK levels are designated on an item-by-item basis.
Context	Context Optional

Reporting Category	PROBABILITY
Content Standard	S.CP CONDITIONAL PROBABILITY AND THE RULES OF PROBABILITY
	Understand independence and conditional probability, and use them to interpret data.
	S.CP.3 Understand the conditional probability of A given B as P(A and B)/P(B), and interpret independence of A and B as saying that the conditional probability of A given B is the same as the probability of A, and the conditional probability of B given A is the same as the probability of B.★
Content Limits	<ul> <li>Items use positive rational numbers to represent probabilities.</li> <li>Items may use Venn diagrams, tree diagrams, or frequency tables.</li> <li>Items may use union and intersection symbols.</li> <li>Conditional probability may be written as a description (i.e., the student identifies events A and B within context and then translates the information into the form A given B) as well as the symbolic notation P(A   B).</li> </ul>
DOK	1, 2, and/or 3 are eligible. DOK levels are designated on an item-by-item basis.
Context	Context Optional

Reporting Category	PROBABILITY
Content Standard	S.CP CONDITIONAL PROBABILITY AND THE RULES OF PROBABILITY
	Understand independence and conditional probability, and use them to interpret data.
	S.CP.4 Construct and interpret two-way frequency tables of data when two categories are associated with each object being classified. Use the two-way table as a sample space to decide if events are independent and to approximate conditional probabilities. For example, collect data from a random sample of students in your school on their favorite subject among math, science, and English. Estimate the probability that a randomly selected student from your school will favor science given that the student is in tenth grade. Do the same for other subjects and compare the results.★
Content Limits	<ul> <li>Items use positive rational numbers to represent probabilities.</li> <li>Items may use Venn diagrams, tree diagrams, or frequency tables.</li> <li>Items may use union and intersection symbols.</li> <li>Conditional probability may be written as a description (i.e., the student identifies events A and B within context and then translates the information into the form A given B) as well as the symbolic notation P(A   B).</li> </ul>
DOK	1, 2, and/or 3 are eligible. DOK levels are designated on an item-by-item basis.
Context	Context Optional

Reporting Category	PROBABILITY
Content Standard	S.CP CONDITIONAL PROBABILITY AND THE RULES OF PROBABILITY
	Understand independence and conditional probability, and use them to interpret data.
	<b>S.CP.5</b> Recognize and explain the concepts of conditional probability and independence in everyday language and everyday situations. For example, compare the chance of having lung cancer if you are a smoker with the chance of being a smoker if you have lung cancer.★
Content Limits	<ul> <li>Items use positive rational numbers to represent probabilities.</li> <li>Items may ask to relate Venn diagrams or tree diagrams to frequency tables.</li> <li>Items may use union and intersection symbols.</li> <li>Conditional probability may be written as a description (i.e., the student identifies events A and B within context and then translates the information into the form A given B) as well as the symbolic notation P(A   B).</li> </ul>
DOK	1, 2, and/or 3 are eligible. DOK levels are designated on an item-by-item basis.
Context	Context Required

Reporting Category	PROBABILITY
Content Standard	S.CP CONDITIONAL PROBABILITY AND THE RULES OF PROBABILITY
	Use the rules of probability to compute probabilities of compound events in a uniform probability model.
	<b>S.CP.6</b> Find the conditional probability of A given B as the fraction of B's outcomes that also belong to A, and interpret the answer in terms of the model.★
Content Limits	<ul> <li>Items use positive rational numbers to represent probabilities.</li> <li>Items may ask to relate Venn diagrams or tree diagrams to frequency tables.</li> <li>Items may use union and intersection symbols.</li> <li>Conditional probability may be written as a description (i.e., the student identifies events A and B within context and then translates the information into the form A given B) as well as the symbolic notation P(A   B).</li> </ul>
DOK	1, 2, and/or 3 are eligible. DOK levels are designated on an item-by-item basis.
Context	Context Optional

Reporting Category	PROBABILITY
Content Standard	S.CP CONDITIONAL PROBABILITY AND THE RULES OF PROBABILITY
	Use the rules of probability to compute probabilities of compound events in a uniform probability model.
	<b>S.CP.7</b> Apply the Addition Rule, P(A or B) = P(A) + P(B) – P(A and B), and interpret the answer in terms of the model.★
Content Limits	<ul> <li>Items use positive rational numbers to represent probabilities.</li> <li>Items may ask to relate Venn diagrams or tree diagrams to frequency tables.</li> <li>Items may use union and intersection symbols.</li> <li>Conditional probability may be written as a description (i.e., the student identifies events A and B within context and then translates the information into the form A given B) as well as the symbolic notation P(A   B).</li> </ul>
DOK	1, 2, and/or 3 are eligible. DOK levels are designated on an item-by-item basis.
Context	Context Optional